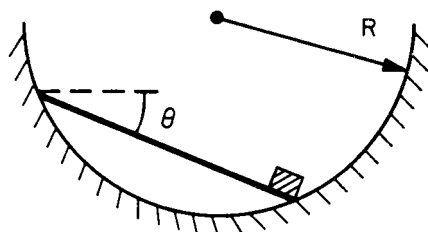
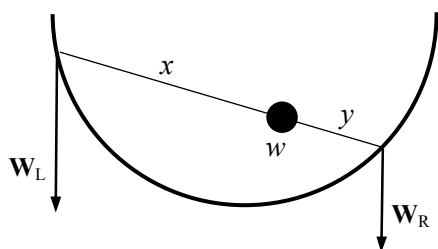
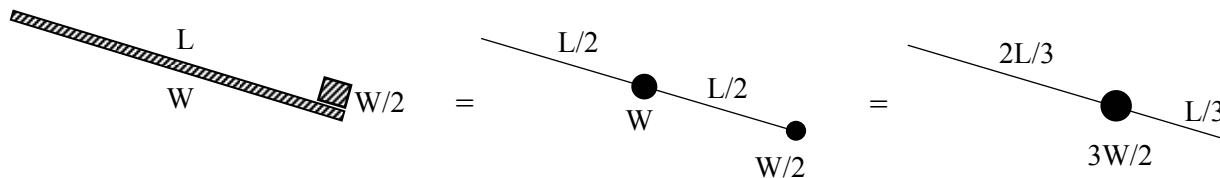


plank weight trough



A plank of weight W and length $\sqrt{3}R$ lies in a smooth circular trough of radius R . At one end of the plank is a weight $W/2$. Calculate the angle θ at which the plank lies when it is in equilibrium.

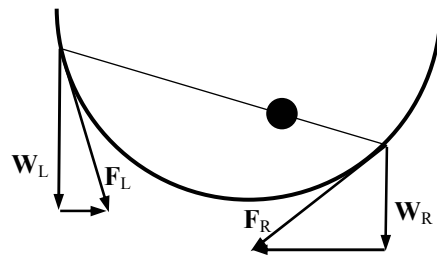
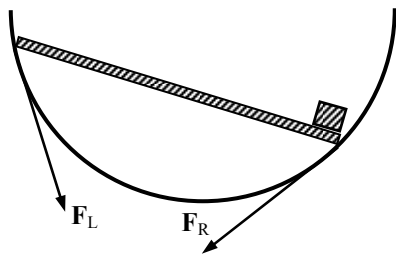
Michael A. Gottlieb's Solution (notes)



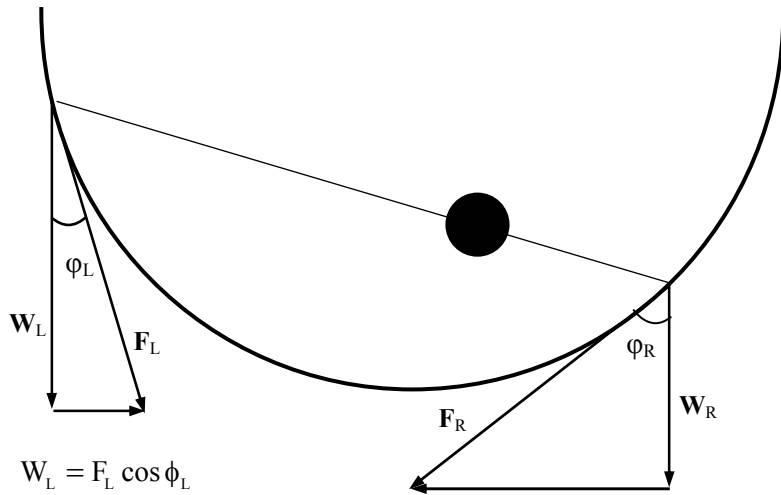
$$W_L = \frac{L/3}{L} (3W/2) \quad W_R = \frac{2L/3}{L} (3W/2)$$

$$W_L = W/2 \quad W_R = W$$

$$W_L = \frac{y}{x+y} w \quad W_R = \frac{x}{x+y} w$$



$F_L = F_R$ at equilibrium



$$F_L = F_R$$

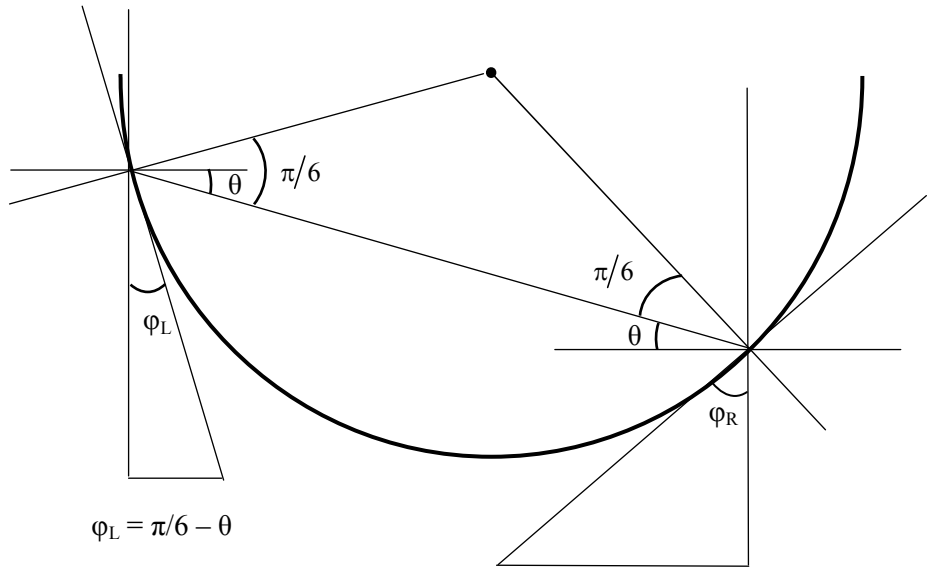
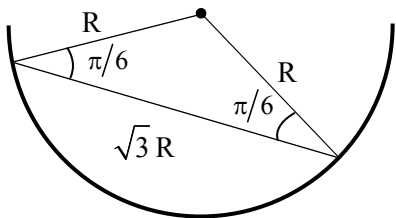
$$\frac{W_L}{\cos \phi_L} = \frac{W_R}{\cos \phi_R}$$

$$\frac{W/2}{\cos \phi_L} = \frac{W}{\cos \phi_R}$$

$$\therefore 2 \cos \phi_L = \cos \phi_R$$

$$W_L = F_L \cos \phi_L$$

$$W_R = F_R \cos \phi_R$$



$$\phi_L = \pi/6 - \theta$$

$$\phi_R = \theta + \pi/6$$

$$2 \cos\left(\frac{\pi}{6} - \theta\right) = \cos\left(\theta + \frac{\pi}{6}\right)$$

$$\therefore \theta = -\frac{\pi}{6}$$